

Math Challenge #10

First Name: _____	Last Name: _____	Grade: _____
Teacher: _____	Parent's email: _____	

Coins and Money Problems

Coin's name	Penny	Nickel	Dime	Quarter	Half Dollar	One Dollar
Value	1 cent	5 cents	10 cents	25 cents	50 cents	100 cents or \$1.00
						

Kinder & First Grade: solve at least 3 problems.
Second & Third Grade: solve at least 7 problems.
Fourth Grade and above: solve at least 12 problems.

	<i>Answer</i>
1. A nickel is a five-cent coin. $5 \text{ cents} + 5 \text{ cents} = 10 \text{ cents}$, which equal to 10 pennies.	<i>10 [pennies]</i>
2. Count up by 5 until you reach 40 to find the number of nickels. Or $40 \div 5 = 8$ nickels	<i>8 [nickels]</i>
3. A gumball cost 25 cents or 5 nickels. The number of coins she has left = $7 - 5 = 2$ coins left	<i>2 [coins left]</i>
4. He gave the store keeper three quarters, which is 75 cents. The store keeper gave him $75 \text{ cents} - 65 \text{ cents} = 10 \text{ cents}$. Since he got 2 coins, the type of coins must be a nickel since it is a five-cent coin.	<i>Nickel</i>
5. Let's think. $80 \text{ cents} \div 4$ is 20 cents. But there is no 20 cent coin, so he will have definitely three 25 cent coins and a nickel (5 cents). You can also guess and check until you arrive with a correct solution.	<i>3 quarters and 1 nickel</i>
6. $18 \text{ dimes} = \$1.80$; $9 \text{ nickels} = \$0.45$. Total value: $\$1.80 + \$0.45 = \$2.25$. There are 9 quarters in \$2.25.	<i>9 [quarters]</i>
7. a. The smallest amount of coins Sonia has is pennies, then there are quarters, the biggest number of coins dimes. She has 6 coins in total, which means she has 1 penny, 2 quarters and 3 dimes. b. $1\text{¢} + 2 \times 25\text{¢} + 3 \times 10\text{¢} = 81\text{¢} = \0.81	<i>a. 2 quarters, 3 dimes and a penny</i> <i>b. 81 cents or 81¢ or \$0.81</i>
8. Work backwards: $50 + 25 = 75$ cents. She had spent half of what she had and was left with 75 cents, so before this, she had \$1.50. She gave half of what she had to her brother and was left with \$1.50, therefore, she must have had \$3. Or draw the model:  $\$0.75$ is a quarter of her original amount, thus Monica had $4 \times \$0.75 = \3 at first.	<i>[\$]3</i>

9.	We can do 'guess and check' or 'make an organized list' of what is possible.	30 [cents] or 30 [¢]
10.	<p>\$3.15 ends on 5, the only way we can get 5 cents at the end is if Josiah has an odd number of quarters.</p> <p>We can make a list with possible number of quarters:</p> <ul style="list-style-type: none"> If Josiah has 3 quarters, the number of dimes on $\\$3.15 - \\$0.75 = \\$2.40$ would be 24. This will not work since we need more quarters than dimes. If Josiah has 9 quarters, the number of dimes on $\\$3.15 - \\$2.25 = \\$0.90$ would be 9. There are the same number of quarters and dimes. If Josiah has 11 quarters, the number of dimes on $\\$3.15 - \\$2.75 = \\$0.40$ would be 4. We have more quarters than dimes. <p>Therefore, the least number of quarters is 11.</p> <p>Another way: \$3.15 ends on 5, the only way we can get 5 cents at the end if Josiah has odd number of quarters. The largest odd number of quarters that fits the sum is 11. $\\$3.15 - 11 \times \\$0.25 = \\$0.40$, or 4 dimes left. $11 > 4$ it works.</p> <p>Let's check the smaller number of quarters, 9.</p> <p>$\\$3.15 - 9 \times \\$0.25 = \\$0.90$ or 9 dimes. In this case, number of quarters equals to the number of dimes.</p> <p>So, the least number of quarters that work is 11.</p>	11 [quarters]
11.	<p>We can do 'guess and check' or 'make an organized list' of what is possible.</p> <p>A football costs \$11 each and a helmet costs \$18 each.</p> <p>Another way to solve it using pictures:</p> <div style="display: flex; align-items: center; margin: 10px 0;">  = \$40 </div> <div style="display: flex; align-items: center; margin: 10px 0;">  = \$47 </div> <p>When we add of the two equations together, we'll get that 3 sets of (football and helmet) costs \$87, so 1 set (helmet + football) cost $\\$87 \div 3 = \\29</p> <p>The cost a football $\\$40 - \\$29 = \\$11$</p> <p>The cost of a helmet $\\$47 - \\$29 = \\$18$</p>	Football: \$11 Helmet: \$18
12.	<p>The number of hours he worked = $\\$1152 \div 12 = 96$ hours.</p> <p>February has 28 or 29 days in total. If we subtract 4 Sundays, we'll get 24 or 25 working days. Possible number of hours work each day: 3×24 days = 72 hours, 4 hours for 24 days = 96 hours.</p> <p>Only 4 hours for 24 fit the conditions.</p>	 <p>4 [hours per day]</p>
13.	<p>One way to solve is to draw a diagram.</p> <div style="display: flex; align-items: center; margin: 10px 0;"> <div style="border: 1px solid black; padding: 5px; margin-right: 10px;">charity $\frac{1}{3}$</div> <div style="border: 1px solid black; padding: 5px; margin-right: 10px; background-color: #d3d3d3;"></div> <div style="border: 1px solid black; padding: 5px; margin-right: 10px;"></div> <div style="border: 1px solid black; padding: 5px; margin-right: 10px;"></div> <div style="border: 1px solid black; padding: 5px;"></div> </div> <p style="margin-left: 150px;">Book $\left[\frac{1}{4} \text{ of } \frac{2}{3} = \frac{2}{12} \text{ or } \frac{1}{6} \right]$</p> <p style="margin-left: 150px;">left [\$45]</p>	

14.	<p>One nickel and one dime have a total value of 15¢. $\\$6 = 600\text{¢}$; 600¢ is divisible by 15¢, which results in 40. Therefore, there were 40 nickels (and 40 dimes).</p> <p>Another way: A set of 10 dimes and 10 nickels is worth \$1.50. Four such sets are worth \$6.00. So, there are 40 nickels and 40 dimes in the \$6.00.</p>	40 [nickels]
15.	<p>Let m = the cost of a mango and b = the cost of a banana. $2m + 3b = 5.60$. So, twice the number of fruits will be $4m + 6b = 11.20$</p> <p>We are given that $4m + 7b = 11.60$.</p> <p>Comparing the two equations ($4m + 6b = 11.20$ and $4m + 7b = 11.60$) tells us that one banana costs $11.60 - 11.20 = \\$0.40$</p> <p>Two mangoes and three bananas cost \$5.60. Since we know a banana cost \$0.40, then a mango costs $(5.60 - 0.40 \times 3) \div 2 = \\2.20.</p> <p>One mango and five bananas will cost $\\$2.20 + 5 \times \\$0.40 = \\$4.20$.</p>	[\$]4.20
16.	<p>If $7/8$ of Geena's money equals to \$2.80, that means $1/8$ of Geena's money must equal to $\\$2.80 \div 7 = \\0.40. Therefore, the total amount of her money ($8/8$) is $\\$0.40 \times 8 = \\3.20.</p> <p>Since Geena had \$1.20 more than Ben, then Ben must have had $\\$3.20 - \\$1.20 = \\$2.00$.</p> <p>The pen cost: $1/4 \times \\$2.00 = \\0.50. Thus, Ben had $\\$2.00 - \\$0.50 = \\$1.50$ left.</p>	[\$]1.50
17.	<p>Based on her specific wants, she would have this set of coins: 1 quarter, 2 dimes, 4 nickels. The value of this set is 65 cents. Since the value of the exchange set is 455 cents, she will get $455/65 = 7$ sets. Since each set contains 1 quarter, therefore the exchange set contained 7 quarters.</p>	7 [quarters]
18.	<p>Notice that the largest amount that can be made is 49 cents. If you experiment with the given set of coins, any amount from 1 cent to 49 cents can be made. Therefore, there are 49 different amounts that can be made.</p>	49 [different amounts]

Solution is available on March 4, 2022, at www.mathinaction.org