
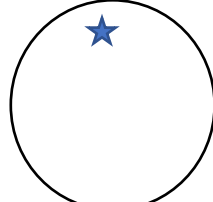
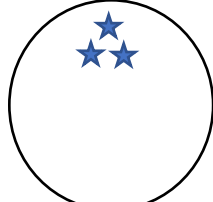
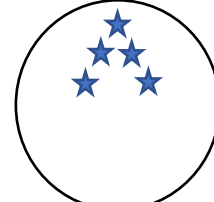


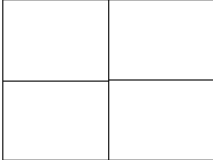
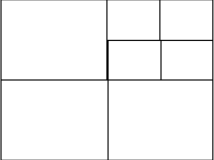
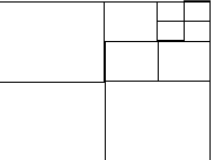


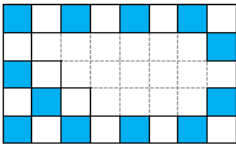
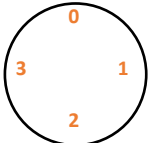




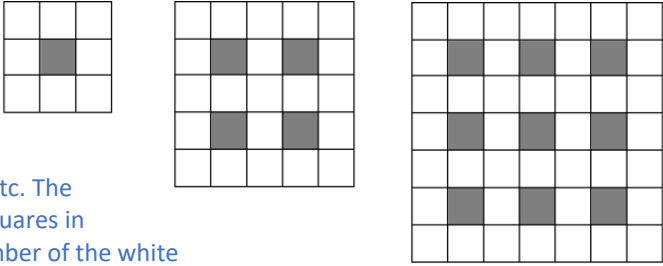
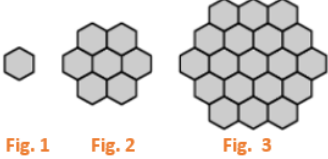
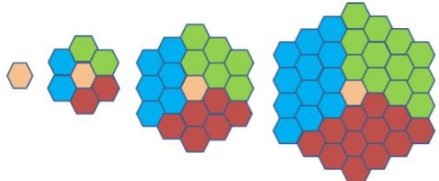
Math Challenge #17

| | | |
|-------------------|-----------------------|--------------|
| First Name: _____ | Last Name: _____ | Grade: _____ |
| Teacher: _____ | Parent's email: _____ | |

Pattern

Kinder & First Grade: solve at least 3 problems.
Second & Third Grade: solve at least 7 problems.
Fourth Grade and above: solve at least 12 problems.

| | <i>Answer</i> |
|---|--------------------|
| <p>1. Josiah arranged the pool balls as shown below. Assuming there are no hidden balls, how many pool balls are there in total?</p>  <p style="margin-left: 100px;">$1+2+3+4+5 = 15$</p> | <i>15</i> |
| <p>2. Jerry bought 12 apples on Sunday and put them in the fridge at home. He brings 1 apple to school on Monday, 2 apples on Tuesday, 3 apples on Wednesday, 4 apples on Thursday, and none on Friday. How many apples will he have left at home by end of the day on Friday?</p> <p>$12 - 1 - 2 - 3 - 4 - 0 = 2$ apples Or you can subtract $(1+2+3+4)$ from 12: $12 - (1+2+3+4) = 12 - 10 = 2$ apples</p> | <i>2 [apples]</i> |
| <p>3. If the pattern continues, how many stars will be in Circle 6?</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>Circle 1</p> </div> <div style="text-align: center;">  <p>Circle 2</p> </div> <div style="text-align: center;">  <p>Circle 3</p> </div> <div style="text-align: center;">  <p>Circle 4</p> </div> </div> <p style="margin-left: 20px;">Each circle has 2 more stars than the previous one. In Circle 5, there will be $7+2 = 9$ stars, and in Circle 6, there will be $9+2 = 11$ stars.</p> | <i>11[stars]</i> |
| <p>4. Tyrone skip-counts by 4 starting with 10. What is the largest number he will say that is less than 50?</p> <p>10, 14, 18, 22, 26, 30, 34, 38, 42, 46, 50</p> | <i>46</i> |
| <p>5. $30+40+50+60+70+80 = 330$</p> | <i>330 [words]</i> |
| <p>6.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>Fig. 1</p> </div> <div style="text-align: center;">  <p>Fig. 2</p> </div> <div style="text-align: center;">  <p>Fig. 3</p> </div> <div style="text-align: center;">  <p>Fig. 4</p> </div> </div> <p style="margin-left: 20px;">The pattern has a difference of 3 between each number: 1, 4, 7, 10, 13, 16, 19, 22, 25, 28, Figure 10 will have 28 tiles.</p> | <i>28 [tiles]</i> |

| | | | |
|-----|--|--|------------------|
| 7. | Notice that every row had 4 blue tiles and 4 white tiles. Now we count how many missing in each row: $3 + 3 + 2 = 8$ tiles. |  | 8 [tiles] |
| 8. | It will happen this millennium, so will start on 20___. The two other digits have to add up to 5. The two digits can be: $2 + 3, 3 + 2, 1 + 4, 4 + 1, 0 + 5, 5 + 0$. The year after 2023 when the sum of the digits is 7 again is 2032 . | 2032 | |
| 9. | Sonja climbs $5 \times 5 = 25$ feet in 15 minutes, while Sawyer climbs $4 \times 3 = 12$ feet in 15 minutes. Sonja climbs $25 - 12 = 13$ ft more than Sawyer | 13 [feet] | |
| 10. |  <p>This clock has a cycle of 4 hours. $50 \div 4 = 12$ R2, so this would be the same as $2 \oplus 2 = 0$ Another way to solve it is to act it out (start at 2 and move 50 steps around the clock).</p> | 0 | |
| 11. | <p>First night </p> <p>Second night </p> <p>Third night </p> <p>Fourth night </p> <p style="text-align: right;">} 890</p> | $890 - (15 \times 6) = 800$ $800 \div 4 = 200$ mosquitoes on the first night Third night: $200 + 15 + 15 =$ 230 mosquitoes | 230 [mosquitoes] |
| 12. | MATHISFUNMATHISFUNMATHISFUN... The pattern repeats after every 9 letters. A multiple of 9 that is the closest to 1002 is 999, which is 111×9 . The 1000 th letter is M, the 1001 st letter is A, and the 1002 nd letter is T. | T | |
| 13. | <p>The side of the big squares increases by 2 (in the figures we have squares with a side of 3, 5, 7, etc.). The black squares (combined) form a smaller square of side 1, 2, 3, etc., so the pattern for the number of the black squares is $1 \times 1, 2 \times 2, 3 \times 3$, etc. The next square will have a side of 9 (81 squares in total) with 4×4 black ones. So, the number of the white ones is $81 - 16 = 65$.</p>  | 65 | |
| 14. | <p>1st figure has 1 hexagon, 2nd figure: $1 + 6 = 7$ hexagons; 3rd figure: $7 + 12 = 19$ hexagons. Notice that we add multiples of 6 each time. Figure 4th: $19 + 6 \times 3 = 37$, and figure 5th: $37 + 6 \times 4 = 61$</p> <p>You may draw it out or notice another pattern.</p>   <p>There is one center piece and 3 identical pieces wrapped around. In the 5th figure you'll have $3 \times 5 \times 4 = 3 \times 20 = 60$ plus 1 centerpiece, or 61 in total.</p> | 61 | |
| 15. | We can look at the pattern that is created on the ones digit: $9 \times 9 = 81$ ends on 1, $1 \times 9 = 9$, ends on 9, $9 \times 9 = 81$ ends on 1 again; it repeats. The pattern is alternating 1 and 9. If we multiply 9 even number of times, we'll get 1 in the ones digit, otherwise 9. We have multiplication of 8 nines, so, it will end on 1. | 1 | |

16. Each time we are adding 2 square tiles to the previous figure.
 To get 150th figure we'll need to add 149×2 to the original figure 1. So, there will be $7 + 149 \times 2 = 305$ square tiles in the 150th figure.

Fig. 1

Fig. 2

Fig. 3

Fig. 4

305 [tiles]

17. One way is to find the pattern.
 Notice that we add 4 new square tiles from one 'h' to the next one. The pattern is 6, 10, 14, and so on. To get to the 4th 'h', we add 4×3 to the first number of tiles, to get to the 5th 'h', we add 4×4 tiles to the first number of tiles, and so on. To get to the 100th 'h', we add 6 to 4×99 : $6 + 4 \times 99 = 402$

402 [square tiles]

18.

Fig. 1

Fig. 2

Fig. 3

The pattern is +7, then +9, +11, +13, ...
 What if we rearrange the shapes (using the same number of tiles):

Fig. 1

Fig. 2

Fig. 3

The first figure has a square with 3 tiles on its sides plus 2 tiles. Figure 2 has a square with 4 tiles on its sides plus 2 tiles, and so on. The 100th figure has a square with 102 tiles on its sides plus 2 tiles.
 The pattern starting with figure 1 will be: $3^2 + 2$, $4^2 + 2$, $5^2 + 2$, and so on.
 Figure 100 will be: $102^2 + 2 = 10,406$ tiles.

10,406 [tiles]

Solution is available on March 17, 2023
www.mathinaction.org